# PACKET B: Horses, forces, and fun with math

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**Note:** Throughout this exercise, we will stop and check in together as a group. Stop when you see:

\*CHECK IN\*\_\_\_

## Exercise II: Are CSA and SMoA different than expected in larger equids?

6a. Through most of evolutionary history, horses had three toes, but those toes varied in size. If a 400kg horse was just standing still, how much weight do you think would be on each leg?

Now estimate very roughly how much weight would be on **the center digit of a single limb** in 1) a horse with three equally-sized toes; 2) a horse where the side digits are ½ the size of the center digit; and 3) a monodactyl (single-toed) horse like Equus. (KISS)

6b. What do you predict for the forces on **just the center digit** of a monodactyl (one-toed) horse vs. a three-toed horse? In which species are the forces higher?

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7. Take 5 minutes and use the small click-together cubes to make larger cubes of 2x2, 3x3, 4x4, 5x5, 6x6 cubes, as assigned by Brianna. Assume that each cube has a length of 1 unit.

- a. Report the length the larger cube you made (e.g., 2 for the 2x2 cube), its surface area, and its volume to Brianna so she can enter into the groups spreadsheet.
- b. While you're waiting for other groups, warm up those math skills with the following: If length is x, write the relationship of:
  - i. Length (L) as a function of length
  - ii. Area (A) as a function of length
  - iii. Volume (V) as a function of length

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- c. Check back in with the entire group to interpret Graph 2 (How length, surface area, and volume increase).
- d. What can we say about how length, volume, and area increase in relation to each other as a cube gets bigger?

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8. What should the slope of a log-log plot be if we want to plot area (y-axis) vs. length (x-axis)?

9. Fill in the expected slopes of the following relationships, under conditions of isometry. Remember that the dependent variable (y-axis) is given first. Area vs. length

Volume vs. length

Length vs. area

SMoA vs. length

Area vs. volume

SMoA vs. volume

10a. If horse A is "bigger" - i.e., has more mass - than horse B, do you expect the cross-sectional area of horse A's bone to be larger, smaller, or the same size relative to horse B? Think back to your first graph.





10b. Will there be a bigger difference in their masses or in their bone cross-sectional area? Explain your reasoning. (Hint: compare the slope of the volume line and the surface area line on your Graph 1)

11. You are about to make a log-log plot of MCIII cross-sectional area (y-axis) vs. body mass (x-axis) in horses. If MCIII scales with isometry, what do you expect the slope of the line to be?

12. In the Excel sheet on your computer, go to the tab "Graph4- log(CSA) vs. Body Mass. Repeat the graphing procedure from Graph 1 on log cross sectional area and log body mass for all twelve equid taxa. What is the slope of the data?

13. In the Excel sheet on your computer, go to the tab "Graph5- log(CSA) vs. Body Mass. (You will have to highlight the log mass column, then hold the "command" button while highlighting the SMoA column.) Repeat the log-log plot for MCIII SMoA vs. body mass. What is the expected slope of the line under conditions of isometry? What is the actual slope of the data?

14. Were your hypotheses of isometry correct?

15. Why would larger equids have a greater resistance to compression and bending than expected if you just scaled up the resistance present in the MCIII of a smaller horse?

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#### Wrap up discussion re: Doing museum collections research

1) What steps do you think took place to put this project together? (E.g.: sending a formal request to borrow the bones)

2) How do other scientists and the public access the results of this study? How would you go about verifying this study?

